# **Energy and Electron Transfer**





Possibilities



### **Energy Requirement**



# Mechanisms

# Radiative Energy Transfer

Trivial ET

# Non-Radiative Energy Transfer

- Resonance ET
- Exchange ET

### Trivial energy transfer (radiative energy transfer)





- no electronic interaction between D\* and A
- D\* emits a quantum of light which is absorbed by A

A physical encounter between A and D\* is not required, the photon must only be emitted in an appropriate direction and the medium must be transparent in order to allow transmission. Non-Radiative Energy Transfer

Exchange Energy Transfer Collisional Energy Transfer Dexter Energy Transfer



 $k_{\text{ET}}$  (exchange) =  $KJ \exp(-2 r_{\text{DA}}/L)$ 

# Exchange Energy Transfer







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### Exchange Energy Transfer

# $k_{\rm ET}$ (exchange) = $KJ \exp(-2r_{\rm DA}/L)$

where K is related to the specific orbital interactions such as the dependence of orbital overlap to the instantaneous orientations of \*D and A.

J is the normalized spectral overlap integral, where normalized means that both the emission intensity  $(I_D)$  and extinction coefficient  $(\varepsilon_A)$  have been adjusted to unit area on the wavenumber scale. It is important that J, by being normalized does not depend on the actual magnitude of  $\varepsilon_A$ .

 $r_{DA}$  is the donor-acceptor separation relative to their van der Waals radii, L

# Non-Radiative Energy Transfer

Dipole-Dipole Energy Transfer Coulombic Energy Transfer Resonance Energy Transfer Förster Energy Transfer

Förster Resonance Energy Transfer (FRET)



# **Resonance Energy Transfer**

The dipole-dipole interaction represents a classical Coulombic interaction so we can make a classical analogy



- the oscillating field of D\* causes the excitation of nearby electronic systems (provided certain resonance conditions are met)
- this is analogous to absorption of a photon by A to generate A\* as a result of coupling between A<sub>e</sub> and and the oscillating electric field of the light wave



# Resonance Energy Transfer



# Exchange vs Coulomb (Singlet-Singlet)



# Exchange vs Coulomb (Triplet-Triplet)



$$k_{\rm D^* \to A} = \frac{8.8 \times 10^{-25} K^2 \phi_{\rm D}}{n^4 \tau_{\rm D} R^6} \int_0^\infty F_{\rm D}(\nu) \epsilon_{\rm A}(\nu) \frac{d\nu}{\nu^4}$$

 $\kappa^2$  mutual orientation of the dipoles in space  $\phi_D$  = quantum yield of donor emission n = refractive index of the solvent  $\tau_D$  = actual donor lifetime

R = distance between donor and acceptor

 $\int_0^\infty F_{\rm D}(\nu)\epsilon_{\rm A}(\nu) \frac{d\nu}{\nu^4} = \text{spectral overlap integral}$ 

 $\int_{0}^{\infty} F_{\rm D}(\nu) \epsilon_{\rm A}(\nu) \frac{d\nu}{\nu^4}$ 

= spectral overlap integral



Förster theory predicts that  $k_{\text{ET}}$  for an energy transfer via dipole-dipole interactions will be proportional to the following quantities:

- The square of the transition dipole moment  $\mu_{D'}$  corresponding to the \*D  $\rightarrow$  D transition.
- The square of the transition dipole moment  $\mu_A$  corresponding to the A  $\rightarrow$  \*A transition.
- The inverse sixth power of the separation between \*D and A (i.e.  $1/R_{DA}^{6}$ ).

Dipole-dipole mechanism will be most favored for \*D and A pairs such that:

• The \*D  $\rightarrow$  D and A  $\rightarrow$  \*A processes correspond to a large (spectral) overlap integral, *J*.

- The radiative rate constant,  $k^{\circ}_{D}$ , is as large as possible.
- The magnitude of  $\varepsilon_A$  is as large as possible.
- There is a small spatial separation between \*D and A.
- There will be a preferred orientation for which energy transfer is most favorable.

### Differences between Förster (dipole-dipole interaction) and Dexter (electron exchange) energy transfer processes

- The rate of dipole-induced energy transfer decreases as R<sup>-6</sup> whereas the rate of exchange-induced transfer decreases as *exp*-(2r/L). Quantitatively, this means that *k*<sub>ET</sub>(exchange) drops to negligibly small values (relative to the donor lifetime) as the intermolecular (edge-to-edge) distance increases more than on the order of one or two molecular diameters (5-10Å)
- The rate of dipole-induced transfer depends on the oscillator strength of the \*D → D and A → \*A radiative transitions, but the rate of the exchange-induced transfer is independent of the oscillator strength of the \*D → D and A → \*A transitions

#### $\mathbf{D}^* + \mathbf{A} \longrightarrow \mathbf{D} + \mathbf{A}^*$

$$k_{\text{ET}} \text{ (total)} \propto \left[ \alpha \left\langle \Psi(D^*)\Psi(A) \right| H_e \left| \Psi(D)\Psi(A^*) \right\rangle^2 \right]$$
  
Electron exchange  
$$+ \beta \left\langle \Psi(D^*)\Psi(A) \right| H_e \left| \Psi(D)\Psi(A^*) \right\rangle^2$$

Electron dipole-dipole interactions

$$k_{ET}$$
 (Dipole-dipole)  $\propto E^2 \approx \left(\frac{\mu_D \mu_A}{R_{DA}^3}\right)^2 = \frac{\mu_D^2 \mu_A^2}{R_{DA}^6}$ 



Distance dependence, when it can be measured accurately, is a basis for distinguishing energy transfer that occurs by dipole–dipole interactions from electron exchange interactions, since the latter generally falls off exponentially with the separation **R**<sub>DA</sub>

 $k_{\rm ET}$  (exchange) =  $KJ \exp(-2 r_{\rm DA}/L)$ 



# Spin Allowed Energy Transfer Processes

 $^{1}D^{*} + A \longrightarrow D + ^{1}A^{*}$  Forster

 $^{3}D^{*} + A \longrightarrow D + ^{3}A^{*}$  Dexter



A Theory of Sensitized Luminescence in Solids, D. L. Dexter, J. Chem. Phys. 21, 836 (1953)

Transfer mechanisms of electronic excitation, Th. Forster, *Discussions Faraday Soc.* 27, 7, (1959)





### **Upconversion Through Triplet-Triplet Annihilation**





F16. 2.—(a) Absorption spectrum of the energy donor (1-acetyl-4-(1-naphthyl) semicarbazide, \_\_\_\_) and the energy acceptor (dansyl-L-prolyl-hydrazide, ----) in ethanol; (b) emission spectrum of the energy donor (\_\_\_\_) and the energy acceptor (----) in ethanol.

In R<sub>DA</sub>

# Making Use of Förster Resonance Energy Transfer





## Need for Triplet Sensitization



### **Triplet Sensitization**



	$E_{\rm S}$	$E_{\mathrm{T}}$	$\tau_{\rm S}$	$ au_{\mathrm{T}}$		
Compound	(kcal r	nol <sup>-1</sup> )	(s)		Conf. $T_1$	$\Phi_{ST}$
Benzene	110	84	$\sim 10^{-7}$	10 <sup>-6</sup>	π,π*	0.2
Acetone	$\sim 85$	$\sim 78$	10 <sup>-9</sup>	$10^{-5}$	n,π*	1.0
Xanthone		74			$\pi,\pi^*$	1.0
Acetophenone	~ 79	74	$10^{-10}$	$10^{-4}$	$n,\pi^*$	1.0
4-CF <sub>3</sub> Acetophenone		71			n,π*	1.0
Benzophenone	$\sim$ 75	69	$10^{-11}$	$10^{-4}$	n,π*	1.0
Triphenylene	83	67	$\sim 5  imes 10^{-8}$	$10^{-4}$	$\pi,\pi^*$	0.9
Thioxanthone	78	$\sim 65$				
Anthraquinone		62			n,π*	1.0
4-Ph-benzophenone	77	61		$10^{-4}$	$\pi,\pi^*$	1.0
Michler's ketone		61				1.0
Napthalene	92	61	$10^{-7}$	$10^{-4}$	$\pi,\pi^*$	0.7
2-Acetonaphthalene	78	59		$10^{-4}$	$\pi,\pi^*$	1.0
1-Acetonaphthalene	76	57		$10^{-4}$	$\pi,\pi^*$	1.0
Chrysene	79	57	$5 \times 10^{-8}$		$\pi,\pi^*$	0.8
Biacetyl	$\sim 60$	55	$10^{-8}$	$10^{-3}$	n,π*	1.0
Benzil	$\sim 59$	54	$\sim 10^{-8}$	$10^{-4}$	n,π*	1.0
Camphorquinone	$\sim$ 55	50	$\sim 10^{-8}$		n,π*	1.0
Pyrene	77	49	$\sim 10^{-6}$		$\pi,\pi^*$	0.3
Anthracene	76	47	$\sim 5  imes 10^{-9}$	$10^{-4}$	$\pi,\pi^*$	0.7
9,10-Dichloroanthracene	$\sim$ 74	40	$\sim 5  imes 10^{-9}$	$10^{-4}$	$\pi,\pi^*$	0.5
Perylene	66	$\sim 35$	$5 \times 10^{-9}$		$\pi,\pi^*$	0.005

 Table 10.3
 Important Parameters for Triplet Photosensitizers

#### HANDBOOK OF PHOTOCHEMISTRY

THIRD EDITION

Marco Montalti Alberto Credi Luca Prodi M. Teresa Gandolfi

with introductory sections by Josef Michl and Vincenzo Balzani

Taylor & Francis



Handbook of Photochemistry





# **Electron Transfer**



### Electron Addition and Removal is Easier in the Excited State than in the Ground State



Ground state (gas phase)

$$D + A \longrightarrow D^{\bullet +} + A^{\bullet -}$$

$$\Delta G_{et} = (IP)D - (EA)A$$

Excited state (gas phase) \*D + A → D<sup>•+</sup> + A<sup>•−</sup> \*ΔG = (IP)<sub>D</sub> - (EA)A - E\*D

**Excited state In solution** 

 $\Delta G_{et} = E_{1/2}^{ox}(D) - E_{1/2}^{red}(A) - E_{exc}(A) + \Delta E_{Coulombic}$ 





Free energy of activation expressed in terms of the free energy of reaction ( $\Delta G$ ) and free energy of activation ( $\Delta G^{\#}$ )

$$k_{\rm et} = k_0 \exp\left(-\frac{\Delta G_{\rm et}^{\ddagger}}{RT}\right)$$



# $\Delta G_{et} = E_{1/2}^{ox}(D) - E_{1/2}^{red}(A) - E_{*}(D) + \Delta E_{Coulombic}$

# **Rehm-Weller Equation**

# Dependence of the electron transfer rate on the driving force $\Delta G^0$ and the free energy of activation $\Delta G^{\ddagger}$

D. Rehm and A. Weller, *Isr. J. Chem.*, *8*, 259, **1970** 



#### **Rehm-Weller Plot**

The value of  $k_{et}$  reaches a plateau value of ~ 2 x 10<sup>10</sup> M<sup>-1</sup>s<sup>-1</sup> after an exothermicity of ~ -10 kcal mol<sup>-1</sup> and the value of  $k_{et}$  remains the diffusion controlled value to the highest negative values of achievable.

### More Rehm-Weller Plots





Figure 2. Plot of the logarithm of the rate constant vs.  $E_{1/2}(Q/Q^+)$  for the quenching of Cr(bpy)33+ by aromatic amines (O), methoxybenzenes (O), and aliphatic amines (A).



#### V. Balzani, et. al., JACS, 100, 7219, 1978





Figure 4. Plot of the logarithm of the rate constant vs.  $E_{1/2}(Q/Q^+)$  for the quenching of Ir(Me2phen)2Cl2+ by aromatic amines (O), methoxybenzenes (•), and aliphatic amines (A).

C. R. Brock, T. J. Myers and D. G. Whitten, et. al., JACS, 97, 2909, 1975



H. Toma and C. Creutz, Inorganic Chemistry, *16*, 545, **1977** 

Figure 3. Plot of the logarithm of the rate constant vs.  $E_{1/2}(Q/Q^+)$  for the

W. F. Libby, J. Phys. Chem., 56, 863, 1952; J. Chem. Phys., 38, 420, 1963;



Willard F. Libby

The Nobel Prize in Chemistry 1960 was awarded to Willard F. Libby "for his method to use carbon-14 for age determination in archaeology, geology, geophysics, and other branches of science".

 $\begin{aligned} & \mathsf{R}^{\bullet+}(\text{solvated}) + \mathsf{R}(\text{solvated}) \to \mathsf{R}(\text{solvated}) + \mathsf{R}^{\bullet+}(\text{solvated}) \\ & \left[ {}^*\!\! \operatorname{Fe}(\operatorname{H}_2\operatorname{O})_6 \right]^{2+} + \left[ \operatorname{Fe}(\operatorname{H}_2\operatorname{O})_6 \right]^{3+} \to \left[ {}^*\!\! \operatorname{Fe}(\operatorname{H}_2\operatorname{O})_6 \right]^{3+} + \left[ \operatorname{Fe}(\operatorname{H}_2\operatorname{O})_6 \right]^{2+} \end{aligned}$ 



The electron jump from R\* to R\*+ is analogous to the electron jump from a HO to a LU that leads to formation of an electronically excited state.

The electron jump is expected to occur "vertically" and to follow the Franck-Condon principle; the geometry of the products formed by an electron transfer would be the same as the geometry of the reactants.

Two types of reorganization occur after the et: (1) an electronic and vibrational reorganization, termed *internal molecular reorganization*; and (2) a solvent reorganization associated with the solvent reorientation to accommodate the new electronic structures termed *external solvent reorganization*.

 $\begin{aligned} & \mathsf{R}^{\bullet+}(\text{solvated}) + \mathsf{R}(\text{solvated}) \to \mathsf{R}(\text{solvated}) + \mathsf{R}^{\bullet+}(\text{solvated}) \\ & \left[ {}^{*}\!\mathsf{Fe}(\mathsf{H}_2\mathsf{O})_6 \right]^{2+} + \left[ \mathsf{Fe}(\mathsf{H}_2\mathsf{O})_6 \right]^{3+} \to \left[ {}^{*}\!\mathsf{Fe}(\mathsf{H}_2\mathsf{O})_6 \right]^{3+} + \left[ \mathsf{Fe}(\mathsf{H}_2\mathsf{O})_6 \right]^{2+} \end{aligned}$ 





#### Electron transfer is a two step process:

- (a) Electron transfer first with no change of nuclear positions (Franck-Condon principle)
- (b) Solvent reorganization

#### **Marcus Model**

The above two step model violates thermodynamic principle conservation of energy.



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#### On the Theory of Oxidation-Reduction Reactions Involving Electron Transfer. I\*

R. A. MARCUS Department of Chemistry, Polytechnic Institute of Brooklyn, Brooklyn, New York (Received July 28, 1955)

A mechanism for electron transfer reactions is described, in which there is very little spatial overlap of the electronic orbitals of the two reacting molecules in the activated complex. Assuming such a mechanism, a quantitative theory of the rates of oxidationreduction reactions involving electron transfer in solution is presented. The assumption of "slight-overlap" is shown to lead to a reaction path which involves an intermediate state  $X^*$  in which the electrical polarization of the solvent does not have the usual value appropriate for the given ionic charges (i.e., it does not have an equilibrium value). Using an equation developed elsewhere for the electrostatic free energy of nonequilibrium states, the free energy of all possible intermediate state are then determined with the aid of the calculus of variations by minimizing its free energy subject to certain restraints. A simple expression for the electrostatic contribution to the free energy of formation of the intermediate state from the reactants,  $\Delta F^*$ , is thereby obtained in terms of known quantities, such as ionic radii, charges, and the standard free energy of reaction.

This intermediate state  $X^*$  can either disappear to reform the reactants, or by an electronic jump mechanism to form a state X in which the ions are characteristic of the products. When the latter process is more probable than the former, the over-all reaction rate is shown to be simply the rate of formation of the intermediate state, namely the collision number in solution multiplied by  $\exp(-\Delta F^*/kT)$ . Evidence in favor of this is cited. In a detailed quantitative comparison, given elsewhere, with the kinetic data, no arbitrary parameters are needed to obtain reasonable agreement of calculated and experimental results.

R. A. Marcus, J. Chem. Phys., 24, 966, 1956.

R. A. Marcus and N. Sutin, *Biochemica et Biophysica Acta*, *811*, 265, **1985**.

R. A. Marcus, Electron transfer Reactions in Chemistry: Theory and Experiment, (Nobel Lecture) Angew. Chem. Int. Ed., 32, 1111, 1993.



R. A. Marcus

#### Rates are expected:

 $\diamond$  to be slow for weakly exothermic reactions,

 to increase to a maximum for moderately exothermic reactions, and then

to decrease with increasing exothermicity for highly
 exothermic et reactions.

# **Evolution of Marcus model**

R. A. Marcus, J. Chem. Phys., 24, 966, 1956.



# The Marcus model



$$k_{\rm et} = k_0 \exp\left(-\frac{\Delta G_{\rm et}^{\ddagger}}{RT}\right)$$

$$\Delta G_{et} = E_{1/2}^{ox}(D) - E_{1/2}^{red}(A) - E_{*}(A) + \Delta E_{Coulombic}$$

$$\Delta G^{\ddagger} = \frac{(\lambda + \Delta G^{\circ})^2}{4\lambda}$$

$$k_{ET} = \kappa \frac{k_B T}{h} \exp\left(\frac{-(\lambda + \Delta G^{\circ})^2}{4\lambda RT}\right)$$

# The re-emergence of the activation barrier ( $\Delta G^{\dagger}$ ) at large negative $\Delta G^{0}$ values



**Marcus Prediction** 





The '*normal* region exists for values of  $-\Delta G^0 < \lambda$ . In this region the rate of electron transfer will *continuously increase* as the exothermicity increases as long as  $-\Delta G^0 < \lambda$  because the value of  $\Delta G^{\ddagger}$  continuously decreases in this "normal" region of reaction exothermicity.

The 'barrierless' region ( $\Delta G^{\ddagger} = 0$ ) at which  $-\Delta G^{0} = \lambda$ . This corresponds to the maximum rate of electron transfer.

The 'inverted' region where  $-\Delta G^0 > \lambda$ . The rate of electron transfer begins to decrease when  $-\Delta G^0 > \lambda$ .



$$k_{et} = A \exp^{-(\Delta G^{\ddagger}/RT)}$$

 $\Delta G^{\ddagger} = (\Delta G^0 + \lambda)^2 / 4\lambda$ 

### **Electron Transfer Involves Two Steps**



The experimental rate constant is limited by the diffusion rate constant in the solvent, it effectively hides the Marcus inverted region. On the right section of the plot the reaction is endothermic and the prediction of the Marcus equation is followed. The Rehm-Weller equation does not make allowance for an inverted region.

#### Marcus prediction vs Weller's experiments



The experimental rate constant is limited by the diffusion rate constant in the solvent, it effectively hides the Marcus inverted region. On the right section of the plot the reaction is endothermic and the prediction of the Marcus equation is followed. The Rehm-Weller equation does not make allowance for an inverted region.

#### Experimental conditions to observe the Marcus "inverted region"?



For most donor-acceptor (DA) systems the inverted region is obscured by the diffusion limit.

This can be circumvented by:

- freezing the donor-acceptor distribution (glassy medium)
- covalently linking the donor and the acceptor
- \* lowering the donor-acceptor interaction (electronic coupling V) so that the maximum rate for  $-\Delta G^0 = \lambda$  is **lower** than the diffusion limit.

Pioneering 1984 Study by Miller and Closs Definitively Proved the Existence of the Inverse Region







**Figure 2.** Plot of rate constant vs. exothermicity for the reaction  ${}^{1*}P-Q \rightarrow P^{+} - Q^{-}$  and for  $P^{+} - Q^{-} \rightarrow P - Q$ , where P = porphyrin and Q = quinone. The B and T after the name of the compounds indicate data obtained in butyronitrile or in toluene, respectively. The maximum uncertainty in any given rate constant is  $\pm 20\%$ .



**Figure 8.** Plot of intracomplex electron-transfer rate between cyt c and cyt  $b_5$  as a function of free energy. Solid line is fit to Marcus' theory,  $\lambda = 0.8v$ .







e 8.  $\Delta G^{\circ}$  dependence of  $k_{\rm b}/k_{\rm dis}$  for backward ET between Ru,<sup>+</sup> and the cation radicals of the aromatic donors. The line is drawn sy viewing.



Fig. 10. The dependence of the CR rate constant  $k_n$  of geminate ion pairs produced by fluorescence quenching reaction on the free energy gap  $-\Delta G_{ip}^0$  in acetonitrile solution.





# The Nobel Prize in Chemistry 1992





The Nobel Prize in Chemistry 1983 was awarded to Henry Taube "for his work on the mechanisms of electron transfer reactions, especially in metal complexes".

The Nobel Prize in Chemistry 1992 was awarded to Rudolph A. Marcus "for his contributions to the theory of electron transfer reactions in chemical systems".

# Photoinduced electron transfer



### Excited state production through back electron transfer



Bioapplications, Light emitting diodes (TV, Computerr, Cell phone screens)

